Formulae You Should Already Know

| CEBoK <br> Module | formula | parameters | usage / comments |
| :---: | :---: | :---: | :---: |
| 8 | $y=a+b x$ | a (y-int), b (slope) | linear CER |
| 8 | $\begin{gathered} y=a x^{b} \\ y=a x^{b}+c \end{gathered}$ | a (coeff), b (exponent), <br> c (y-int); plot $\ln Y$ vs. $\ln X$ | learning curve power CER |
| $\begin{aligned} & \hline 5 \\ & 8 \end{aligned}$ | $\begin{aligned} y=a e^{b x} & =a k^{x}=a(1+r)^{n} \\ y & =a e^{b x}+c \end{aligned}$ | a ( $y$-int), b (slope), r (rate); plot $\ln \mathrm{Y}$ vs. X | exponential growth exponential CER |
| 8 | $y=a+b \ln x$ | a (y-int), b (slope, log space); plot $Y$ vs. $\ln X$ | logarithmic CER |
| 3 | $y=a+b x+c x^{2}+\cdots$ |  | polynomial CER |
| 8 | $S S E+S S R=S S T$ | Error + Regression = Total | ANOVA sums of squares |

## Formulae You Will Be Given (or not)

| CEBoK <br> ref | formula | parameters | usage / comments |
| :---: | :---: | :--- | :--- |
| 8 | $b=\frac{\sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)\left(Y_{i}-\bar{Y}\right)}{\sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)^{2}}$ |  | OLS regression slope <br> ("easy to remember") |
|  | $b=\frac{\sum_{i=1}^{n} X_{i} Y_{i}-n \bar{X} \bar{Y}}{\sum_{i=1}^{n} X_{i}^{2}-n \bar{X}^{2}}$ | "four-column table": X, <br> $\mathrm{Y}, \mathrm{X}^{2}, \mathrm{XY}$ | OLS regression slope <br> ("easy to compute") |

## Test-Taking Tips

- Time management: Work quickly but not hastily. Skip tough problems and come back to them later.
- Eliminate answers: If you can eliminate certain answers as implausible, you'll increase your chances, even if you have to guess.
- Work backward from answers: On a multiple-choice test, it is sometimes easier to test each answer to see whether it works than to solve directly for the correct answer.
- Look for "sanity checks": Is your numerical answer reasonable when compared with the problem inputs? Use intuition, numeracy, or rules of thumb. If you're doing inflation, costs should be higher in the future and lower in the past; weighted indices should be greater than raw indices. If you're doing learning curve, CUMAV should produce steeper learning than Unit Theory with the same nominal LCS.
- Always guess! There is no penalty for guessing. Never leave a question blank.

Formulae to Memorize for the Exam

| CEBoK <br> Module | formula | parameters | usage / comments |
| :---: | :---: | :---: | :---: |
| 5 | $D T \cdot r \approx 70$ (or 72) | $\begin{array}{\|l\|l} \hline \text { DT = doubling time } \\ r=\text { interest rate (in } \\ \text { percentage points) } \\ \hline \end{array}$ | the "Rule of 70 " or "Rule of 72" |
| 6 | $\begin{aligned} & s^{2}=\frac{\sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)^{2}}{n-1} \\ & s^{2}=\frac{\sum_{i=1}^{n} X_{i}^{2}-n \bar{X}^{2}}{n-1} \end{aligned}$ | "two-column table": $X, X^{2} ; n=$ number of data points, $\mathrm{n}-1=$ degrees of freedom | sample variance <br> ("easy to remember") <br> sample variance <br> ("easy to compute") |
| 7 | $\begin{gathered} L C S=2^{b} \\ b=\log _{2} L C S \end{gathered}$ | LCS = learning curve slope, $b=\log$ space slope | improvement factor applied for doubling |
| 7 | $\begin{aligned} & L M P \approx \frac{\frac{F+L}{2}+\sqrt{F L}}{2} \\ & L M P \approx \frac{F+L+2 \sqrt{F L}}{4} \end{aligned}$ | LMP = lot midpoint <br> F = first unit \# of lot <br> L = last unit \# of lot | Lot Midpoint heuristic |
| 7 | $\begin{aligned} & \text { LMP } \\ & \approx\left[\frac{(L+1 / 2)^{b+1}-(F-1 / 2)^{b+1}}{N(b+1)}\right]^{1 / b} \end{aligned}$ | ```LMP = lot midpoint N = L-F+1 = # units in lot b= log space slope``` | Lot Midpoint approximation (aka Asher's Approximation) |
| 8 | $\begin{gathered} R^{2}=\frac{S S R}{S S T} \\ R^{2}=1-\frac{S S E}{S S T} \end{gathered}$ | R = Pearson's product moment coefficient SSX = sums of squares | ANOVA Coefficient of Determination |
| 8 | $\begin{aligned} & \hat{Y} \pm t_{(n-1)-k, \frac{\alpha}{2}} \\ & \cdot S E E \sqrt{\frac{1}{n}+\frac{(X-\bar{X})^{2}}{\sum_{i=1}^{n} X_{i}^{2}-n \bar{X}^{2}}} \end{aligned}$ | Y-hat = regression line prediction at $X$ $\mathrm{t}=$ right-tail probability $\mathrm{n}=$ \# data points | Confidence Interval (OLS Regression) |
| 8 | $\begin{aligned} & \hat{Y} \pm t_{(n-1)-k, \frac{\alpha}{2}} \\ & \cdot S E E \sqrt{1+\frac{1}{n}+\frac{(X-\bar{X})^{2}}{\sum_{i=1}^{n} X_{i}^{2}-n \bar{X}^{2}}} \end{aligned}$ | k= \# ind. variables <br> alpha $=$ significance <br> SEE = std err of estimate <br> $X$-bar $=$ mean of $X$ | Prediction Interval(OLS Regression) |
| 10 | $\begin{gathered} \operatorname{Cov}(X, Y)=E\left[\left(X-\mu_{X}\right)\left(Y-\mu_{Y}\right)\right] \\ \operatorname{Cov}(X, Y)=E[X Y]-\mu_{X} \mu_{Y} \end{gathered}$ | $\begin{aligned} & \text { mu-sub- } X=\text { mean of } X \\ & \text { mu-sub- } Y=\text { mean of } Y \end{aligned}$ | Covariance of two random variables |
| 10 | $\operatorname{Var}(\mathrm{X})=\left(\mathrm{a}^{2}+\mathrm{b}^{2}+\mathrm{c}^{2}+-\mathrm{ab}-\mathrm{ac}-\mathrm{bc}\right) / 18$ | $a=\text { low, } b=\text { most likely, }$ c=high | Variance of triangular distribution |
| 11 | $\text { Std Time }=\frac{\text { Measured Time } \cdot \text { Pace }}{1-P F \& D}$ | PF\&D = Personal <br> Fatigue and Delay | time standards |
| 15 | $E A C=A C W P+\frac{B A C-B C W P}{T C P I}$ | $\begin{aligned} & \text { BAC = Budget At Compl } \\ & \text { TCPI = future cost } \end{aligned}$ | general EAC formula |
| 15 | $T C P I_{L R E}=\frac{B A C-B C W P}{L R E-A C W P}$ | performance: <br> CPI ("best case"), <br> CPI * SPI ("worst | rearrangement of general EAC formula |


|  |  | case"), |  |
| :--- | :--- | :--- | :--- |
|  | $0.8 C P I+0.2$ SPI, etc. |  |  |

## Formulae Not to Memorize (Just Understand the Concept)

| CEBoK <br> Module | formula | parameters | usage / comments |
| :---: | :---: | :---: | :---: |
| 2 | $\begin{aligned} & C_{2}=\left(\frac{T_{2}}{T_{1}}\right) C_{1} \\ & C_{2}=\left(\frac{C_{1}}{T_{1}}\right) T_{2} \end{aligned}$ | $\begin{aligned} & \mathrm{C}=\text { cost } \\ & \mathrm{T}=\text { technical (scaling } \\ & \text { parameter) } \end{aligned}$ | analogy technique <br> "dollars-per-ton" |
| 2 | $y=C_{1}+b\left(x-T_{1}\right)$ |  | adjusted analogy <br> ("borrowed" slope) |
| 3 | $y=a+\left[C_{1}-\left(a+b T_{1}\right)\right]+b x$ |  | calibrated CER |
|  | weighted average $\bar{x}=\frac{\sum_{i=1}^{n} w_{i} x_{i}}{\sum_{i=1}^{n} w_{i}}$ | w = weights (usually sum to one) | composite index [5] <br> comp. labor rate [11] <br> ESLOC [12] <br> UAC [13] <br> Award Fee [14] |
| 7 | $L M P=\left(\frac{\sum_{i=F}^{L} i^{b}}{N}\right)^{1 / b}$ | $\mathrm{N}=\mathrm{L}-\mathrm{F}+1$ | Lot Midpoint formula (exact) |
| 7 | $T C_{N}=a N^{b+1}$ | $\mathrm{a}=\mathrm{T} 1$ | total cost (CUMAV) |
| 7 | $U C_{k}=a k^{b+1}-a(k-1)^{b+1}$ | b = log space slope | unit cost (CUMAV) |
| 8 | $a=\bar{Y}-b \bar{X}$ | $\begin{aligned} & a=y \text {-intercept } \\ & b=\text { slope } \end{aligned}$ | OLS regression y-intercept |
| 8 | $\begin{gathered} \text { d.f. }(S S E)=(n-1)-k \\ \text { d.f. }(S S R)=k \\ \text { d.f. }(S S T)=n-1 \end{gathered}$ | k = \# variables <br> (excluding y -intercept) | ANOVA degrees of freedom |
| 6 | $C V=\frac{S_{Y}}{\bar{Y}}$ | $s=$ standard deviation | coefficient of variation (univariate) |
| 8 | $C V=\frac{S E E}{\bar{Y}}$ | SEE = standard error of the estimate | coefficient of variation (bivariate) |
| 8 | $\ln y=\ln a+b \ln x$ | plot $\ln \mathrm{Y}$ vs. $\operatorname{In} \mathrm{X}$ | power in log space |
| 8 | $\ln y=a+b x$ | plot $\ln \mathrm{Y}$ vs. X | exponential in semi-log space |
| 9 | $C G F=\frac{\text { Final Cost }}{\text { Initial Cost }}$ |  | Cost Growth Factor |
| 9 | $S G F=\frac{\text { Final Schedule }}{\text { Initial Schedule }}$ |  | Schedule Growth Factor |
| 11 | $F_{R}=\frac{\text { Actuals }}{\text { Standard }}$ |  | Realization Factor |
| 11 | $F_{E}=\frac{\text { Standard }}{\text { Actuals }}$ |  | Efficiency Factor |
| 13 | $N P V=P V_{B}-P V_{C}$ | B = Benefits, C = Costs | Net Present Value |


| 13 | $P V=\frac{F V}{(1+i)^{n}}$ | FV = Future Value | Present Value (year-end indices) |
| :---: | :---: | :---: | :---: |
| 13 | $P V=\frac{F V}{(1+i)^{n-\frac{1}{2}}}$ | $\mathrm{i}=$ discount rate <br> $\mathrm{n}=$ number of years | Present Value (mid-year) indices) |
| 13 | $0=\sum \frac{C F_{t}}{(1+r)^{t}}$ | CF = cash flow | Internal Rate of Return (solve for $r$ ) |
| 14 | $P T A=T C+\frac{C P-T P}{G S_{\text {over }}}$ | $\begin{aligned} & \text { CP }=\text { Ceiling Price } \\ & \text { TP }=\text { Target Price } \\ & \text { GS }=\text { Government Share } \end{aligned}$ | Point of Total Assumption |
| 14 | $\begin{aligned} & R I E_{\text {low }}=T C-\frac{M F-T F}{C S_{\text {under }}} \\ & R I E_{\text {high }}=T C+\frac{T F-m F}{C S_{\text {over }}} \end{aligned}$ | MF = Maximum Fee <br> $\mathrm{mF}=$ Minimum Fee <br> CS = Contractor Share | Range of Incentive Effectiveness |
| 14 | $\text { Margin }=\frac{F e e}{1+\text { Fee }}$ |  | Return On Sales (ROS) |
| 14 | $F e e=\frac{\text { Margin }}{1-\text { Margin }}$ |  | Return On Cost (ROC) |
| 15 | $C V=B C W P-A C W P$ | BCWP = Budgeted Cost | Cost Variance |
| 15 | $S V=B C W P-B C W S$ | of Work Performed | Schedule Variance |
| 15 | $C P I=\frac{B C W P}{A C W P}$ | ACWP = Actual Cost... <br> BCWS = Budgeted Cost | Cost Performance Index |
| 15 | $S P I=\frac{B C W P}{B C W S}$ | of Work Scheduled | Schedule Performance Index |

