# A Second Generation Upgrade to Anderlohr's Retrograde Method for Broken Learning

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# **About the Author**

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#### Education

- SAS/Analytics Certificate, Texas A&M
- M.Stat, Econometrics, University of Utah
- B.S. Applied Mathematics with Econ Emphasis, Weber State University

### Certifications

- PMP
- CCEA

### Experience:

- Cost Estimation (Operations Research): 17 years
- Tecolote Research Inc.
  - Air Force ICBM Directorate
  - NASA Constellation Program
  - Navy SSP

### Background

- Task: Develop LCCE for a component upgrade
- RDT&E to be performed by the acquisition team

### Production

- LRIP performed by acquisition team (2 buys)
- FRP performed by sustainment team (multiple buys)

### Important Assumptions

- Bona fide need
  - Production Rate X unit per year
  - Production Requirement X/10 units per year (i.e. limited deployment capacity)
- The contractor used for LRIP may be distinct from that of FRP (i.e. cannot be assumed to be the contractor)
- Corollary Assumptions
  - There will be production gaps
  - The cost improvement rates experienced in LRIP may not manifest in FRP

# Background (cont'd)

#### Initial Methodology

- Estimated the learning rate based on historical programs
- Employed retrograde method to model the lost learning
- Anderlohr's method to estimate the level of lost learning
  - Personnel Learning
  - Supervisory Learning
  - Continuity of Productivity
  - Methods
  - Special Tooling
  - Example:

| Category                      | Weight | Percent<br>Lost | Weighted<br>Loss |
|-------------------------------|--------|-----------------|------------------|
| Personnel                     | 25%    | 75%             | 18.8%            |
| Supervisory                   | 20%    | 20%             | 4.0%             |
| Continuity of Production      | 20%    | 50%             | 10.0%            |
| Tooling                       | 15%    | 25%             | 3.8%             |
| Methods                       | 20%    | 50%             | 10.0%            |
| Total Loss of Learning Factor | 100%   |                 | 46.5%            |

# **Review of Retrograde Technique**

#### Learning Curve Equation

- UC = AX<sup>b</sup>
- Where
  - A = Theoretical First Unit (TFU)
  - X = The number of the production unit in question
  - b = Ln(slope)/Ln(2)

### Problem Illustration

- TFU = 100 hours
- Learning Slope = 80%
- Production Break at the 10<sup>th</sup> unit



# **Review of Retrograde Technique (cont'd)**

#### Illustration: Retrograde Solution

 Incorporating 45% loss of gained efficiencies yields an equivalent of 7 units of retrograde



### **Review of Retrograde Technique (cont'd)**

#### Illustration: The math

- Efficiencies gained:  $UC_1 UC_{10} = 100 47.7 \approx 52.4$
- Lost Efficiency (from Anderlohr's technique): 0.465 \* 52.4 ≈ 24
- Hours for the 11<sup>th</sup> unit would have been 46, but now they equal: 46 + 24 = 70  $\approx$  UC<sub>3</sub>
- The number of retrograde units = 7

### Equation of Curve after the break

- $UC_{1,X} = UC_{0,(X-K)}; X \ge F$ 
  - UC = Unit Cost
  - X = X<sup>th</sup> production Unit
  - K = Units of Retrograde + 1
  - F = First Unit after Break

• 
$$UC_{1,11} = UC_{0,(11-8)} = UC_{0,3}$$



# **Problem Illustration**

- When the post-break slope (b<sub>1</sub>) does not equal the pre-break slope (b<sub>0</sub>)
  - UC<sub>1,11</sub> = A<sub>0</sub>(X − K)<sup>b0</sup>
    - $A_0(X-K)^{b0} = 100 * 3^{(ln(.80)/ln(2))} = 70.2$ , given original slope
    - $A_0 (X-K)^{b1} = 100 * 3^{(ln(.90)/ln(2))} = 84.6$ , given the new slope



# **Common Solution**

- By changing the learning slope after the break, we must necessarily relax the condition UC<sub>1,X</sub> = UC<sub>0,(X − K)</sub> for X ≥ F
- We recognize that the important condition is that the proper level of learning is lost. So we treat the pre and post-break curves as distinct equations and set the initial condition
  - UC<sub>1, F</sub> = UC<sub>0, F K</sub>
- With only one unknown  $(A_1)$  we can solve the equation
  - $A_1 F^{b1} = A_0 (F K)^{b0}$
  - $A_1 = A_0 (F K)^{b0} / F^{b1}$
- The Post-Break equation becomes
  - $UC_{1, X} = [A_0 (F K)^{b0} / F^{b1}]X^{b1}; X \ge F$

### **Common Solution (cont'd)**

As expected the amount of lost learning is calculated correctly and the post-break slope follows the new learning slope

![](_page_10_Figure_3.jpeg)

### **A Problem with the Solution**

■  $UC_{1,X} \neq UC_{0,(X-K)}$  for X > F when the slope remains unchanged

![](_page_11_Figure_3.jpeg)

### **Second Generation Upgrade: Problem Statement**

- Using the common solution, <u>the rate of change</u> at the first unit after the production break, does not equal <u>the rate of change</u> at the equivalent unit prior to the production break when the learning slope remains unchanged
  - $UC'_{0, F-K} \neq UC'_{1, F}$

# Second Generation Upgrade

- Conditions for the Second Generation Upgrade
  - UC<sub>0, F K</sub> = UC<sub>1, F</sub>
  - UC'<sub>0, F-K</sub> = UC'<sub>1, F</sub>
- Finding the derivatives of UC<sub>0</sub> and UC<sub>1</sub> are straight forward
  - $UC'_{0, F-K} = A_0 b_0 (F-K)^{(b0-1)}$
  - $UC'_{1, F} = A_1 b_1 F^{(b1-1)}$
- Expanding the equations for the first condition yields
  - $A_1 F^{b1} = A_0 (F K)^{b0}$
- Expanding the equations for the second condition yields
  - $A_1 b_1 F^{(b1-1)} = A_0 b_0 (F K)^{(b0-1)}$

This gives us 2 equations and 2 unknowns. Solving them yields

- $A_1 = A_0 (F K) \frac{b0}{F} (F K)$
- $b_1 = b_0 F / (F K)$

# Second Generation Upgrade (cont'd)

This upgrade offers a more aggressive learning slope relative to the retrograde solution

![](_page_14_Figure_3.jpeg)

![](_page_15_Picture_1.jpeg)

# **Peripheral Topics**

### **Challenges to the Technique**

- From the solution we calculate
  - $b_1 = b_0 F / (F K)$
- Since F > 0 and K > 0 it necessarily follows that  $F/(F K) \ge 1$
- Since  $b_0 \le 0$ ,  $b_1 \le b_0$  (i.e.  $b_1$  is more negative than  $b_0$ )
- This means that the slope of the post-break curve is at least as aggressive than the slope of the pre-break curve

![](_page_16_Figure_7.jpeg)

# Challenges to the Technique (cont'd)

The chart illustrates that the steepness of the slope changes mildly for small K, but increases dramatically as K approaches F.

![](_page_17_Figure_3.jpeg)

# **Possible Application**

New plant, or additional production line, the loss of learning is inevitable, but some have argued that the new production line should "catch up" to the original line.

![](_page_18_Figure_3.jpeg)

![](_page_19_Picture_1.jpeg)

![](_page_19_Picture_2.jpeg)