



# Cost-Risk Analysis "Best Practice Mathematically



 Each simulation trial results in a set of values for spacecraft subsystems masses, subsystems power loads, and corresponding set of values for subsystems costs

$$\begin{split} M_{SC}^i &= \left\{ m_j^i \right\} = \left\{ m_{Str}^i , m_{Th}^i , m_{Propulsion}^i , m_{EPS}^i , m_{ADS}^i , m_{ACS}^i , m_{Com}^i , m_{CDH}^i \right\} \\ P_{SC}^i &= \left\{ p_j^i \right\} = \left\{ p_{Str}^i , p_{Th}^i , p_{Propulsion}^i , p_{EPS}^i , p_{ADS}^i , p_{ACS}^i , p_{Com}^i , p_{CDH}^i \right\} \\ \varepsilon_{SC}^i &= \left\{ \varepsilon_j^i \right\} = \left\{ \varepsilon_{Str}^i , \varepsilon_{Th}^i , \varepsilon_{Propulsion}^i , \varepsilon_{EPS}^i , \varepsilon_{ADS}^i , \varepsilon_{ACS}^i , \varepsilon_{Com}^i , \varepsilon_{CDH}^i \right\} \\ X_{SC}^i &= \left\{ X_j^i \right\} = \left\{ X_{Str}^i , X_{Th}^i , X_{Propulsion}^i , X_{EPS}^i , X_{ADS}^i , X_{ACS}^i , X_{Com}^i , X_{CDH}^i \right\} \end{split}$$

The total "simulated" spacecraft system dry mass, power requirement, and cost estimate

$$M_{SC\,Total}^i = \textstyle \sum_{j=1}^8 m_j^i \qquad P_{SC\,Total}^i = \textstyle \sum_{j=1}^8 p_j^i \quad X_{SC\,Total}^i = \textstyle \sum_{j=1}^8 X_j^i$$

$$X_{j}^{i} = f_{j}(m_{j}^{i}p_{j}^{i}) * \varepsilon_{ij}$$

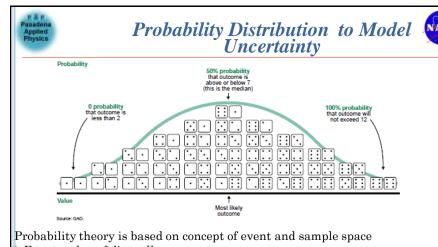
> The probability of occurrence of each simulation outcome

$$\forall i, f(M_{SC}^i, P_{SC}^i, \varepsilon_{SC}^i, X_{SC}^i) = \frac{1}{n} \neq 0$$

The Cumulative Density Function

$$F\left(M_{SC}^{i},P_{SC}^{i},\varepsilon_{SC}^{i},X_{SC}^{i}\right) = \sum_{X_{SC}^{k} \leq X_{SC}^{i}} f\left(M_{SC}^{k},P_{SC}^{k},\varepsilon_{SC}^{k},X_{SC}^{k}\right)$$

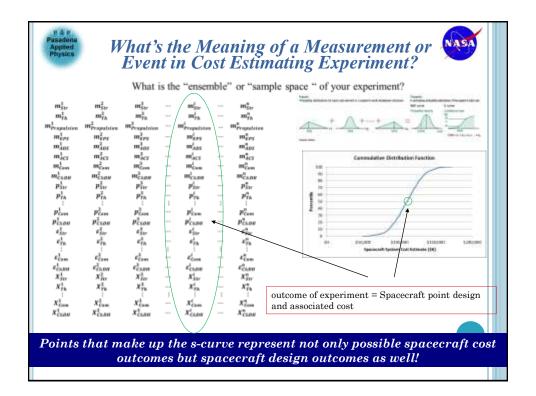




Event: value of dice roll Sample space: all possible value outcomes associated with rolling a pair of dice

➤36 possible outcomes > Normalization condition is met:  $\int_{-\infty}^{+\infty} f(s)ds = \int_{0}^{12} f(s)ds = 1$ 

Probability theory is based on the concepts of event and sample space which must be defined before one can attempt to model uncertainty using probability distribution



P & P Pasadona Applied Physics



### There is a Problem....

- ➤ Technical design parameters of spacecraft subsystems are <u>interdependent</u>, <u>analytically</u> and <u>implicitly</u> related to one another via key physical relationships
- ➤ These key physical relationships are generally not upheld when cost analysts perform cost-risk simulations
- ➤ The generated spacecraft point designs (i.e., simulated sets of CER input variables) based on subjective statistics may be neither technically feasible nor buildable (i.e., "Frankenstein" designs)
- ➤ Yet all simulation design outcomes are assigned non-zero probability of occurrence and, consequently, the resulting spacecraft system cost CDF is invalid
- The resulting cost-risk assessment may be too high or too low

Design parameters of spacecraft subsystems are related to one another via key physical relationships which are generally NOT upheld in cost-risk simulations



# Cost-Risk Analysis "Best Practice" Violates Laws of Physics...



> Rocket equation:

$$m_{prop} = M_{SC\,Total}^{i} \left[ e^{\left( \Delta V / l_{Sp} \theta \right)} - 1 \right],$$

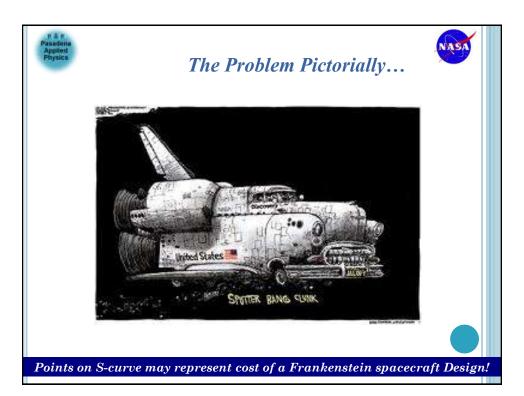
> Solar array sizing equation:

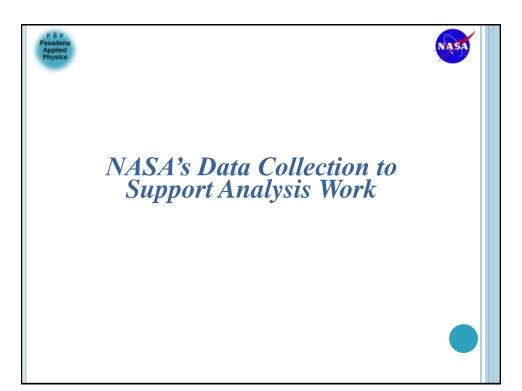
$$A = \frac{P_{EOL}}{F_S f_p \varepsilon_{BOL} (1.0 - \delta_{los}) [1.0 - \gamma_T (t_0 - t_{REF})] \cos(\alpha) \, (1.0 - \beta)^T} \,, \label{eq:alpha}$$

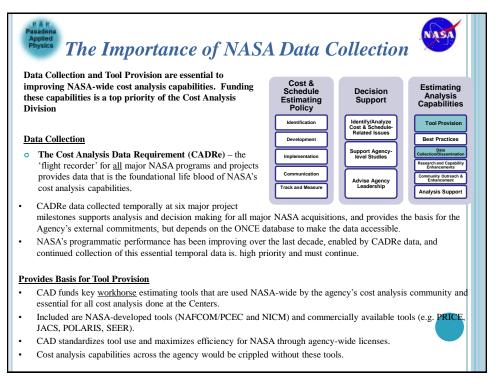
➤ Stefan-Boltzmann law:

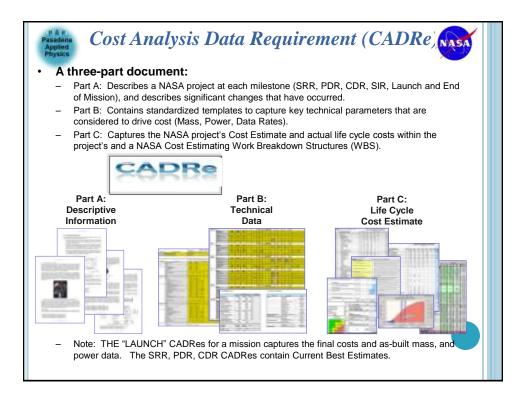
$$A = \frac{Q}{\sigma T^4},$$

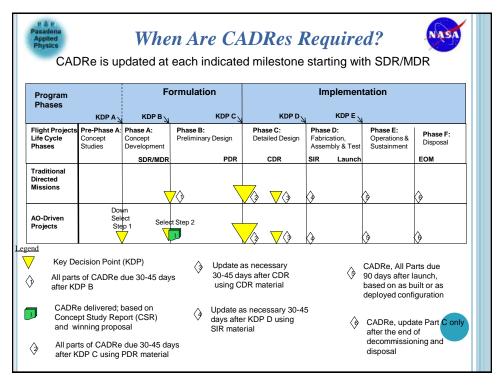
Some of the randomly generated spacecraft point designs based on subjective statistics are not technically feasible, buildable, or flyable. Yet they are assigned non-zero probability of occurrence and consequently costrisk assessment is invalid

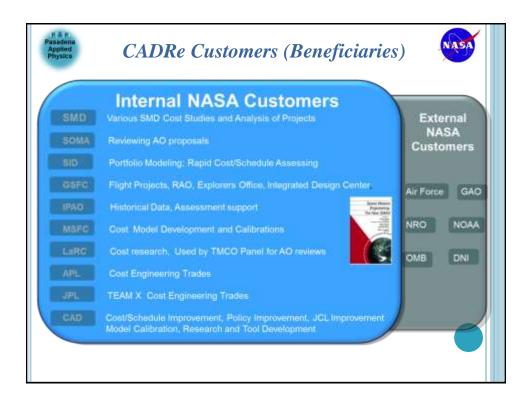


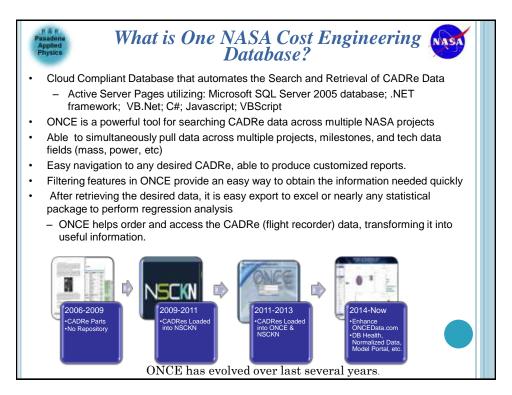


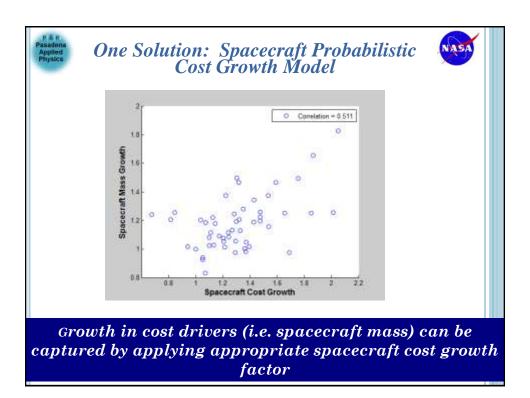














#### Spacecraft Probabilistic Cost Growth Model in a Nutshell



- ➤ Model does not require cost driver uncertainty input
- ➤ Requires only two parameters:
  - ➤ Current Best Estimate(CBE) of spacecraft system cost
  - ➤ CBE maturity relative to project milestones, which is reasonably objective
- ➤ Based on historical analogous systems (available in NASA CADRe database)
- ➤ Predicts spacecraft system cost growth (or shrinkage)
- ➤ Produces cost growth factor distribution result (embodies uncertainty) that recognizes the possibility of growth or shrinkage of cost driver (i.e. spacecraft design parameters)

Provides probabilistic cost growth adjustment to spacecraft cost CBE

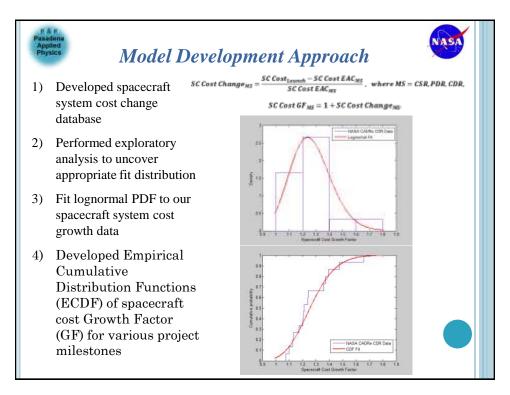


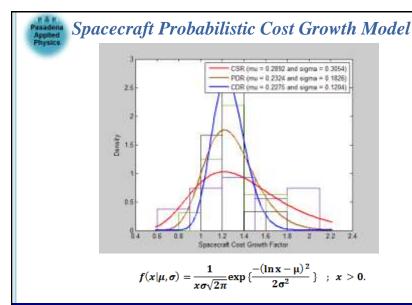
## Study Dataset



NASA Project	CSR/SRR	PDR	CDR
CONTOUR	N/A	Х	Х
MESSENGER	Х	Х	Х
New Horizons	Х	Х	Х
STEREO	Х	Х	Х
AIM	X	X	X
AQUA	X	X	X
CHIPSat	X	X	N/A
EO-1	Х	N/A	Х
GLAST	Х	X	Х
IBEX	X	X	X
LRO	N/A	X	X
RHESSI	X	X	X
SWAS	Х	X	Х
Terra	X	X	X
TRACE	X	N/A	N/A
TRMM	Х	Х	Х
CloudSat	Х	X	Х
MRO	Х	Χ	X
Spitzer	Х	Х	X

19 Earth-Orbiting and Deep Space Missions Obtained from NASA CADRe Database





Decreasing mean growth factor and growth factor uncertainty (decreasing CV) as estimate relative maturity increases



### Methodology: Spacecraft System Cost Growth Adjusted S-Curve



- Determine spacecraft subsystem cost drivers (mass or other key technical parameters) and obtain their CBE values
- 2. Plug these values in the appropriate spacecraft subsystem CERs, ignoring their contingency values
- Develop cost probability distributions of spacecraft subsystems to model uncertainty associated with the cost methodology only
- 4. Account for correlation between costs of various spacecraft subsystems
- 5. Perform simulation, use the "rollup procedure" and generate the overall spacecraft system cost distribution
- Select the appropriate spacecraft cost growth factor distribution based on where in the mission development life cycle the spacecraft cost CBE is being generated.
- Adjust the resulting spacecraft cost probability distribution by combining it with the selected spacecraft cost growth factor distribution
- Use the resulting cost probability distribution to assess the percentile or "confidence" level associated with a point estimate
- Recommend sufficient cost reserves to achieve the percentile or level of "confidence" acceptable to the project or organization
- 10. Allocate, phase, and convert a risk-adjusted cost estimate to then-year dollars





#### **Conclusions**



- ➤ Cost analysts need to understand that while spacecraft design parameters are not typically known with sufficient precision, their uncertainties should NOT be modeled with subjective distributions
  - ➤ Let's not abuse theory of probability! Know what you are simulating, define your event and sample space
- > Spacecraft subsystem design parameters are analytically and implicitly related by physical and engineering relationships
- One suggested solution is probabilistic growth cost model which embodies cost driver uncertainty
- > System-of-systems cost models should ensure the validity of their input vectors
- ➤ Be wary of traditional cost estimate S-curve, it's just a measure of an individual's belief
- ➤ We will always lack the normalization condition unless we find a way to apply Quantum Field Theory in cost-risk analysis!!!

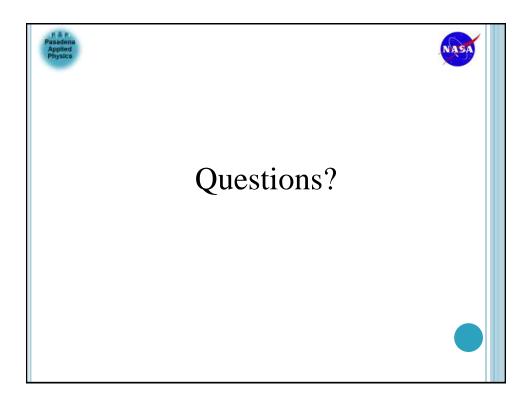


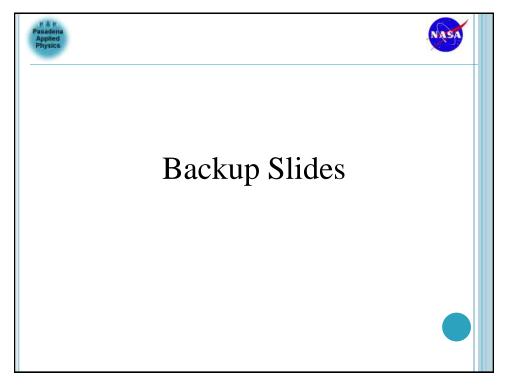
# References

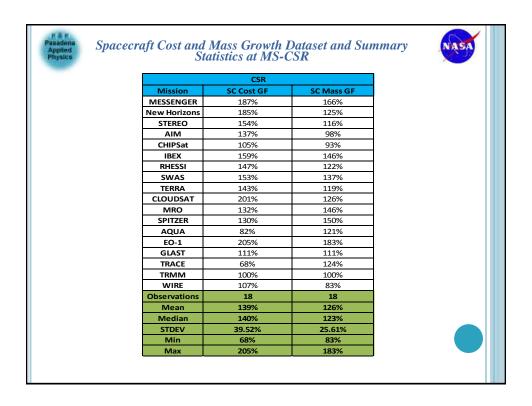


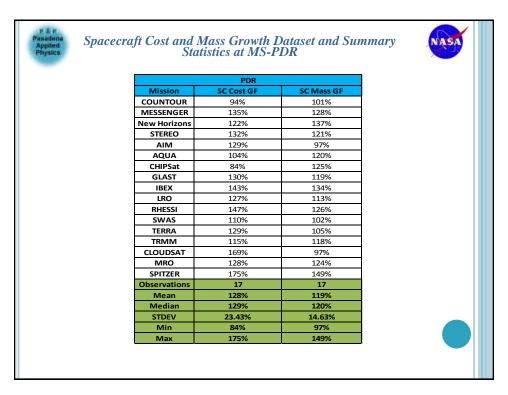
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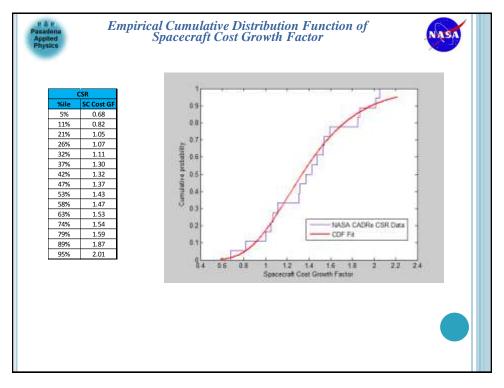


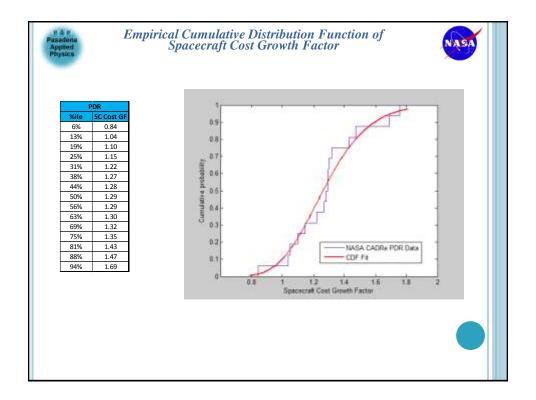


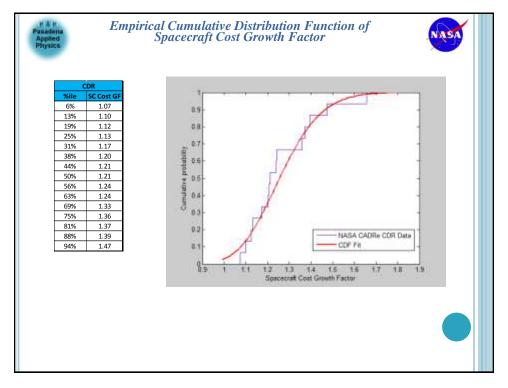




	CDR		
Mission	SC Cost GF	SC Mass GF	
COUNTOUR	105%	94%	
MESSENGER	133%	113%	
New Horizons	107%	119%	
STEREO	124%	112%	
AIM	139%	101%	
AQUA	121%	105%	
EO-1	137%	105%	
GLAST	110%	108%	
IBEX	112%	122%	
LRO	120%	108%	
RHESSI	147%	120%	
SWAS	121%	101%	
TERRA	113%	102%	
TRMM	117%	109%	
CLOUDSAT	136%	100%	
MRO	124%	108%	1
SPITZER	166%	125%	_
Observations	17	17	
Mean	126%	109%	
Median	121%	108%	
STDEV	15.91%	8.45%	
Min	105%	94%	
Max	166%	125%	









# Value Added Benefits of CADRe for Projects and Research



#### **Before CADRe:**

- NASA had <u>no</u> repository of historical project programmatic, schedule, cost, and technical data.
- Programmatic history of NASA projects were not captured systematically.
- Cost Estimates were developed <u>without</u> understanding past history, so quality of cost estimates suffered.
- Cost Research efforts were limited and inconclusive without meaningful data.
- In family checks against other completed projects was difficult and not readily performed with any consistency.
- When cost data was collected, the data was not made available for other project estimating exercises.

#### With CADRe:

- NASA now has a generous repository of specific Cost, Technical, Schedule data to support cost estimating for future projects.
- NASA can now better evaluate future AO proposals to help determine which proposals are in family with history and better explain reasons for differences.
- Helps NASA PM record in a formal agency document key events that occurred during the project (both internal & external).
- Helps PMs understand relevant heritage and previous risk postures, and schedule durations when building their own baselines
- CADRe allows for performing advanced cost research which was not possible previously (ie, Optimum Cost Phasing, Expl of Change, Dashboard Sheets).